



## Exercises: Interaction and Concurrency

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### 1 Basics

The goal of the following exercise is to develop mathematical intuition, helpful in quantum computation.

1. Consider the following matrices:

$$Id = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}; X = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}; Y = \begin{bmatrix} 0 & -i \\ i & 0 \end{bmatrix}; Z = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}; S = \begin{bmatrix} 1 & 0 \\ 0 & i \end{bmatrix};$$
$$H = \begin{bmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & \frac{-1}{\sqrt{2}} \end{bmatrix}$$

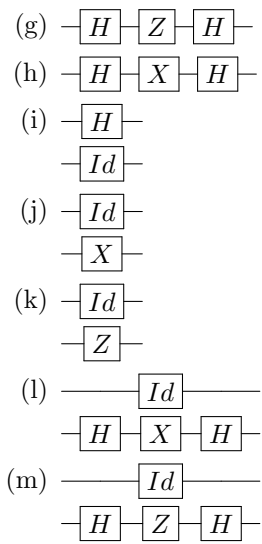
Determine each of the following:

- (a)  $Y \cdot S$
- (b)  $S \cdot S$
- (c)  $X \cdot X$
- (d)  $H \cdot H$
- (e)  $H \otimes Id$
- (f)  $Id \otimes X$
- (g)  $H \cdot Z \cdot H$
- (h)  $H \cdot X \cdot H$
- (i)  $Id \otimes (H \cdot X \cdot H)$
- (j)  $Id \otimes (H \cdot Z \cdot H)$

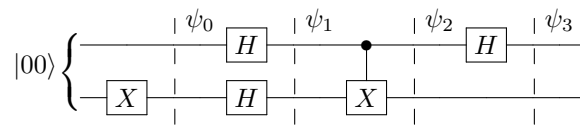
### 2 Introduction to quantum computation

1. If possible associate each of the following circuits to the letters of exercise 1 section 1.

- (a)  $\boxed{Y} \boxed{S}$
- (b)  $\boxed{X} \boxed{X}$
- (c)  $\boxed{H} \boxed{H}$
- (d)  $\boxed{Id}$
- (e)  $\boxed{X}$
- (f)  $\boxed{Z}$



2. Recall dirac's notation T10.



Write each  $\psi$  in dirac's notation.